

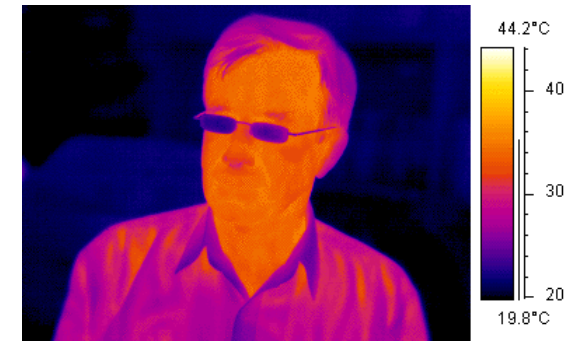
Thermal radiation

In the case of heated objects, a faint reddish light can be observed when the temperature reaches about 525 °C, and then upon further heating they glow yellow or white, i.e. they emit light (electromagnetic waves in the visible range).



- So with increasing temperature the spectrum **shifts** to shorter wavelengths and the emitted **power rapidly increases**.

Although we can only see the radiation of very hot bodies with our own eyes, we can also measure the radiation of bodies at lower temperatures with the help of instruments. Every object whose temperature is not absolute zero radiates.

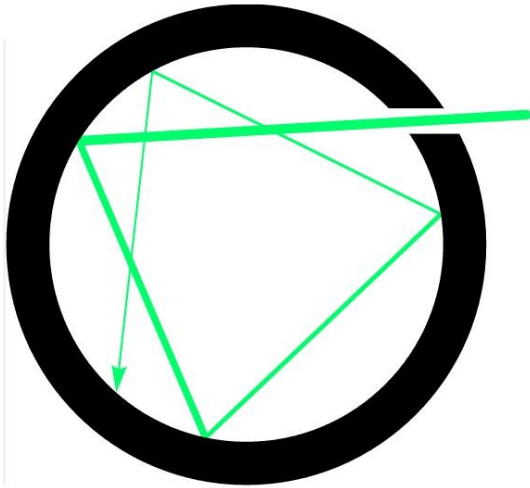


Thermal radiation is also called blackbody radiation.

Ideal black body: one that completely absorbs the radiation incident on it, and the radiation emitted depends only on the temperature. This can be achieved with a hollow body made of any material and a small hole in it, because it is true for a hole that all

- the radiation incident on it enters the cavity through the hole.
- the light reflected from the inner wall of the cavity most likely remains inside and is absorbed inside.
- thermodynamic equilibrium is established between the electromagnetic radiation and the material.
- the spectrum of the radiation then depends only on the temperature of the material.

Generation of thermal radiation

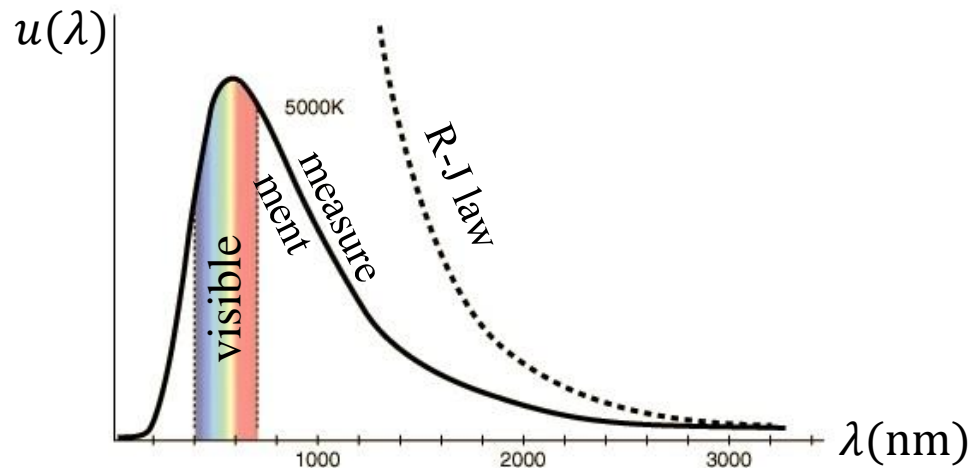


A large number of oscillators in the wall of the material perform irregular vibrations at all kinds of frequencies.

Emission: vibrating charges emit radiation, which includes all kinds of frequencies and therefore wavelengths.

Absorption: radiation incident on a material causes oscillators with the appropriate natural frequency to resonate, so they absorb energy from the radiation.

Rayleigh-Jeans law: taking into account this interaction between radiation and matter, the classical spectral energy density derived using Maxwell's equations tends to infinity for short wavelengths (ultraviolet catastrophe).



Oscillators with quantized energy

Planck (1900): the energy of an oscillator with frequency f cannot be a continuous arbitrary value, but an integer number times the ε energy quantum.

$$\varepsilon = hf \quad \text{where } h \text{ is the Planck's constant: } h = 6,626 \cdot 10^{-34} \text{ Js}$$

This assumption meant the beginning of **quantum physics**.

He obtained the following for the emission as a function of λ (spectral energy density):

$$u(\lambda, T) = \frac{8\pi hc}{\lambda^5} \frac{1}{e^{hc/(\lambda kT)} - 1} \quad \text{where } k \text{ is Boltzmann's constant: } k = 1,38 \cdot 10^{-23} \text{ J/K}$$

Wien's displacement law: differentiating $u(\lambda, T)$ with respect to the wavelength the position of the peak:

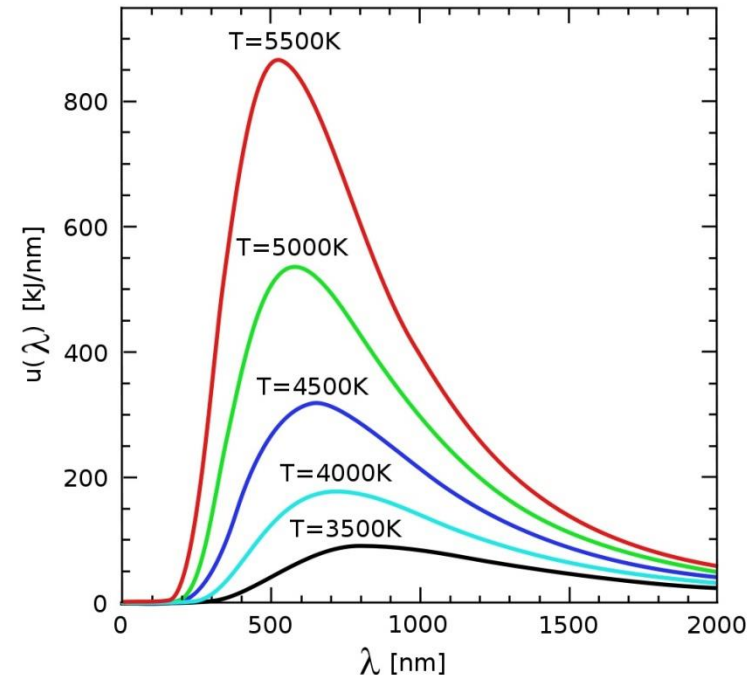
$$\lambda_{max} \cdot T = \text{constant}$$

The Wien constant is $2,9 \cdot 10^{-3} \text{ Km}$.

Stefan-Boltzmann law: integrating the $u(\lambda, T)$ with respect to the wavelength (area under curve) we get the total radiated power. An ideal blackbody with T temperature and A surface area:

$$P = \sigma \cdot T^4 \cdot A$$

where $\sigma = 5,67 \cdot 10^{-8} \text{ W}/(\text{m}^2 \cdot \text{K}^4)$ is the Stefan-Boltzmann constant.



Pressure caused by light

Intensity: energy reaching a unit area perpendicular to the direction of light per unit time

$$I = \frac{E}{tA} = \frac{Nhf}{tA} = \frac{Nhc}{tA\lambda}$$

Change in momentum for one photon:

- when absorbed $|\overrightarrow{\Delta p_f}| = h/\lambda$
- when reflected $|\overrightarrow{\Delta p_f}| = 2h/\lambda$

The pressure exerted by light on an absorbing surface:

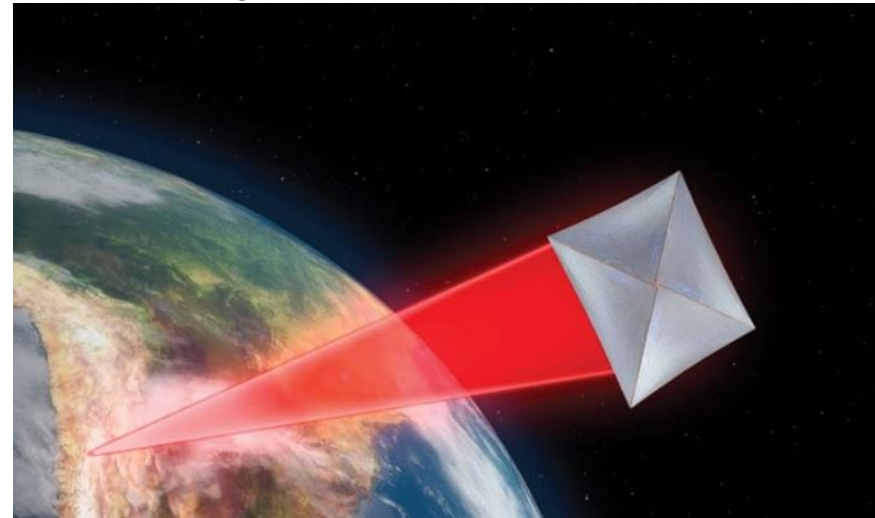
$$p = \frac{F}{A} = \frac{|\overrightarrow{\Delta p}|/t}{A} = \frac{N|\overrightarrow{\Delta p_f}|}{tA} = \frac{Nh}{tA\lambda} = \frac{I}{c}$$

for reflecting surface: $p = \frac{2I}{c}$



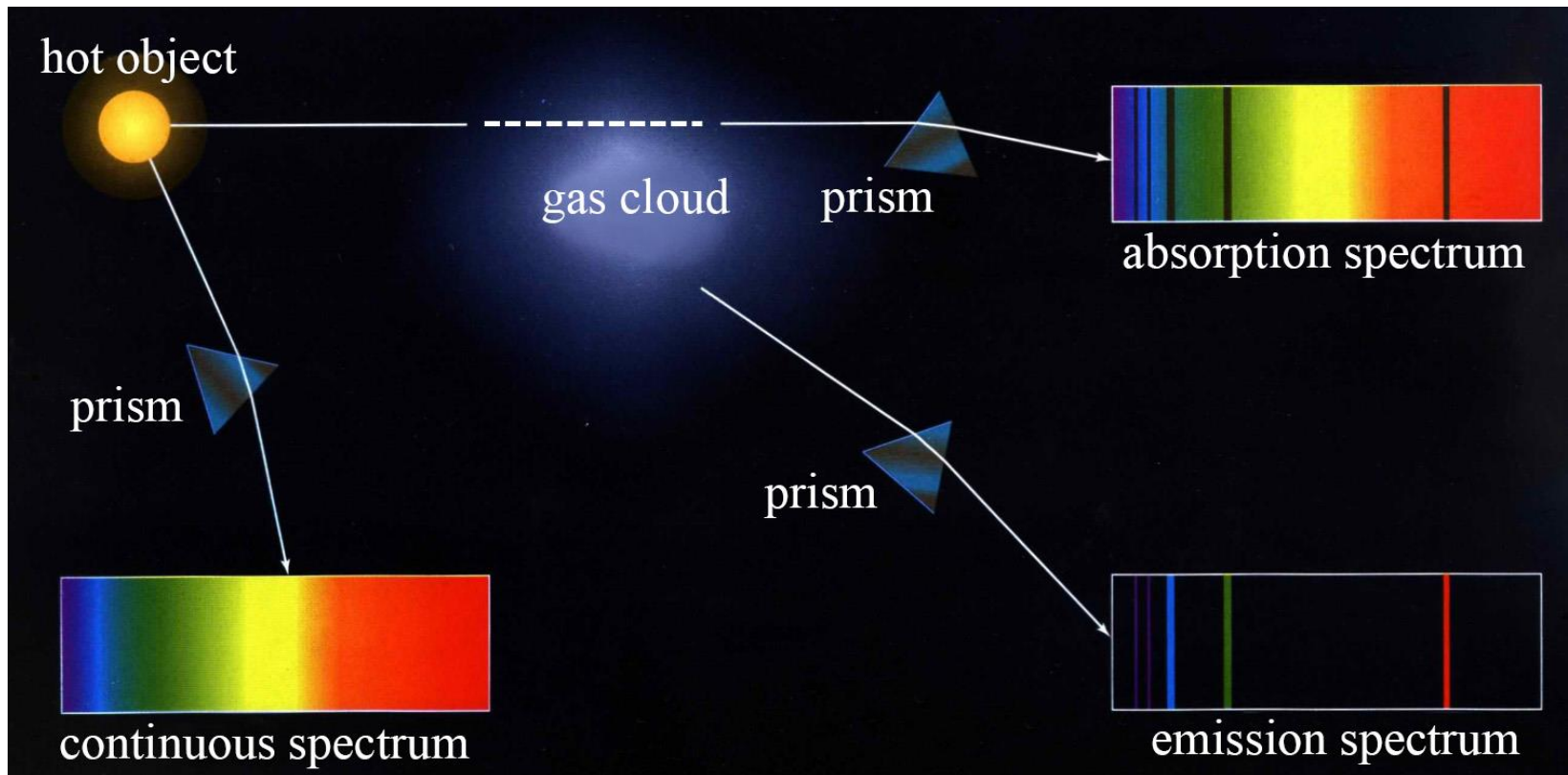
one side
absorbs light,
other side
reflects:
spun up
by pressure
difference

Breakthrough Starshot



Emission and absorption spectra of gases

In contrast to the continuous spectrum thermal radiation of a solid body, atomic gases or vapors only emit and absorb radiation at certain frequencies.



The lines of the spectrum can be used as a kind of fingerprint and with their help distant celestial bodies can be identified.

Explanation of the spectra of gases – Bohr's postulates

From the emitted and absorbed photons with well-defined frequencies, it can be concluded that only certain energy transitions are possible in atoms.

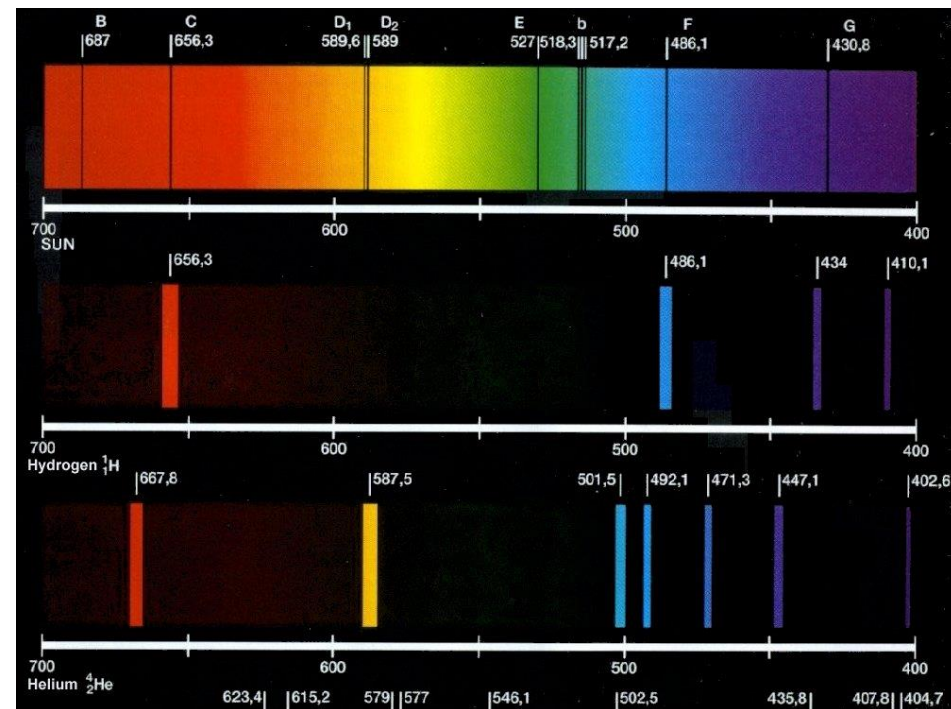
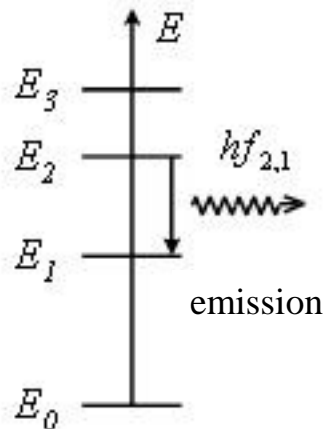
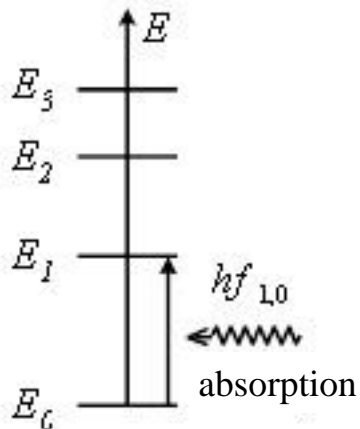
Bohr's postulates:

- In atoms, electrons reside only in discrete energy levels E_1, E_2, \dots, E_i and do not radiate in these stationary orbits.
- Atoms only emit radiation when an electron moves from a higher energy orbit to a lower one.

The inverse of emission is absorption.

Bohr's frequency condition:

$$E_i - E_j = hf_{ij}$$



Bohr model of the hydrogen* atom

The model must provide the discrete E_n energies of the electron.

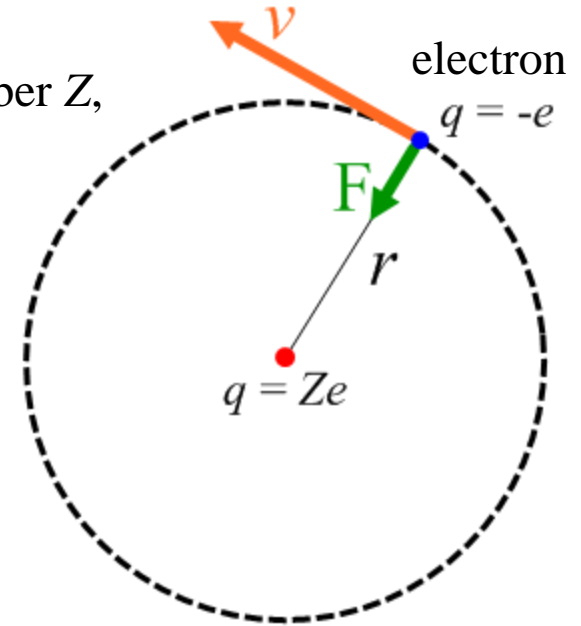
The orbital angular momentum of the electron: $L = mvr$

Like energy, this is also quantized: $L = nh/(2\pi) = n\hbar$

*Not only good for hydrogen, but also for ions with atomic number Z , which contain only one electron (hydrogen-like):

$$\frac{kZe^2}{r^2} = m \frac{v^2}{r} \rightarrow kZe^2 = mvr \cdot v = n\hbar \cdot v$$

$$v = \frac{kZe^2}{n\hbar}$$



The total (mechanical) energy of the electron:

$$E = E_{kin} + E_{pot} = \frac{1}{2}mv^2 - \frac{kZe^2}{r} = \frac{1}{2}mv^2 - mv^2 = -\frac{1}{2}mv^2$$

$$E_n = -\frac{1}{2}mv_n^2 = -\frac{mk^2Z^2e^4}{2\hbar^2} \frac{1}{n^2} = -E^*Z^2 \frac{1}{n^2}$$

$$E^* = \frac{m_0e^4k^2}{2\hbar^2} = 2,176 \cdot 10^{-18} \text{ J} = 13,6 \text{ eV}$$

($m = m_0$: rest mass of electron)

(ionization energy of hydrogen)

Energy levels of the hydrogen atom

From the previously derived formula, we obtain the energy levels of hydrogen for $Z = 1$:

$$E_n = -E^* \frac{1}{n^2} \qquad E^* = \frac{m_0 e^4 k^2}{2\hbar^2} = 2,176 \cdot 10^{-18} \text{ J} = 13,6 \text{ eV}$$

For emission and absorption frequencies:

$$f_{nm} = \frac{E_n - E_m}{h} = \frac{E^*}{h} \left(\frac{1}{m^2} - \frac{1}{n^2} \right)$$

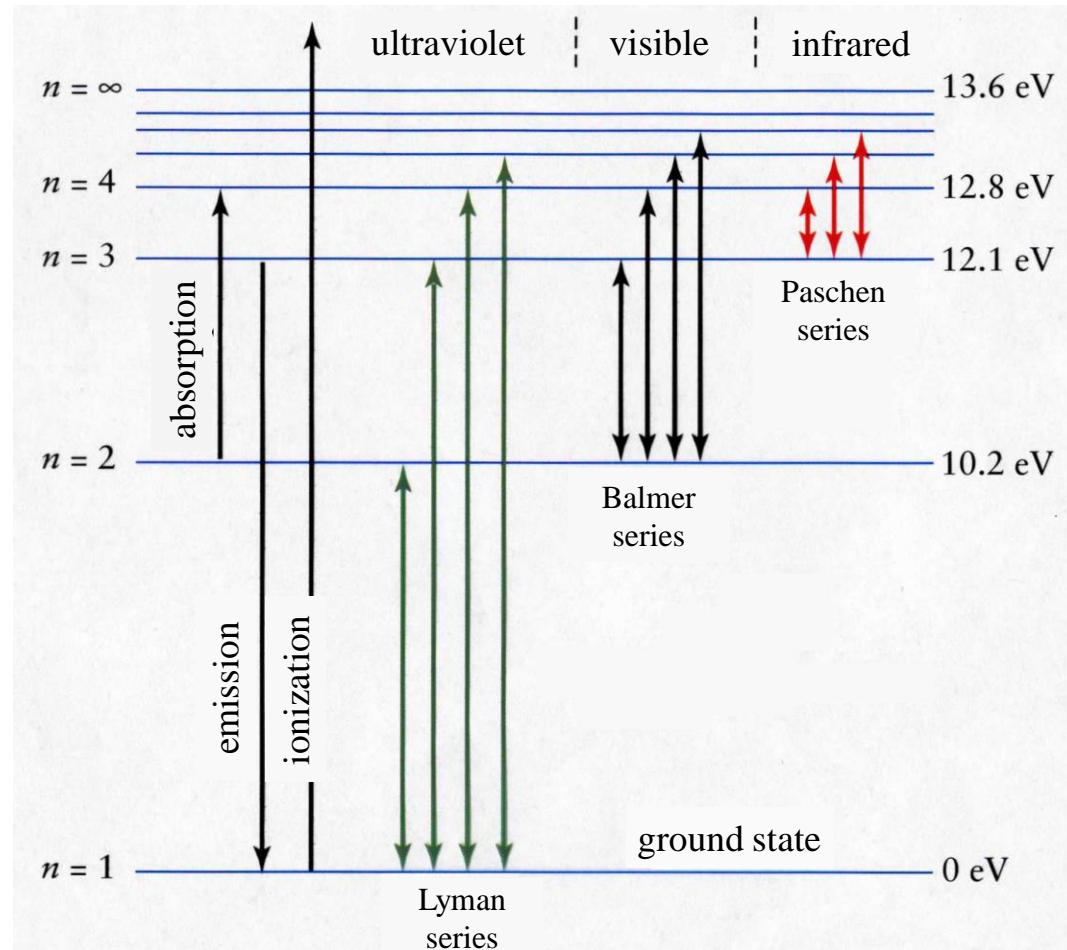
$$f_{nm} = R \left(\frac{1}{m^2} - \frac{1}{n^2} \right)$$

R : Rydberg constant

Lyman series: $f_{n1} = R \left(1 - \frac{1}{n^2} \right)$

Balmer series: $f_{n2} = R \left(\frac{1}{4} - \frac{1}{n^2} \right)$

Paschen series: $f_{n3} = R \left(\frac{1}{9} - \frac{1}{n^2} \right)$



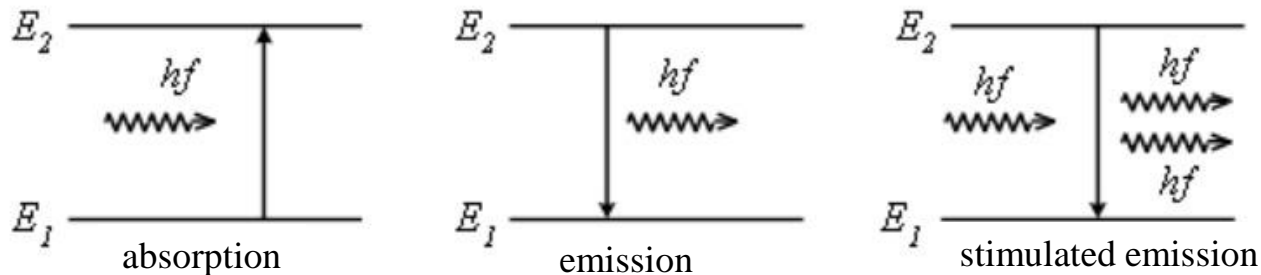
Excited state of atoms - Stimulated emission

By absorbing a photon of the appropriate energy, the atom enters an excited state, and the given electron jumps to a higher energy orbit. This is the process of **absorption**.

The lifetime of the excited state is about 10^{-8} s, but there also exist metastable states with approximately 10^{-3} s lifetime!

Then, through **spontaneous emission**, the electron jumps to a lower energy state with the emission of a photon of appropriate energy: $E_2 - E_1 = hf$

Einstein predicted a third type of process in 1916, **stimulated emission**.



Stimulated emission:

In the case of stimulated emission, de-excitation and emission do not occur spontaneously, but are triggered (**stimulated**) by a photon of the same energy passing by the excited atom. The emitted photon travels in the same direction as the inducing photon, and has the same frequency, phase, and plane of polarization, so the two photons are **coherent**.

Operation of laser

LASER: **L**ight **A**mplification by **S**timulated **E**mission of **R**adiation

Stimulated emission makes it possible to amplify light.

Operation: By pumping energy, they achieve that there are more electrons in the excited state than in the low energy state (**population inversion**). Then there will be more stimulated emission than absorption, so the light is amplified.

Properties: monochromaticity (same frequency), low divergence, high coherence, high surface power density (can be enhanced with lenses), high spectral power density (since there is only one frequency).

Applications of lasers:

- machining, drilling, spot welding,
- surgical intervention, eye surgery
- gene surgery,
- barcode reading,
- CD player laser reading head,
- interference-based length and speed measurement,
- direction setting,
- holography



X-rays

The wavelength of X-rays falls in the range between 10^{-11} and 10^{-8} m.

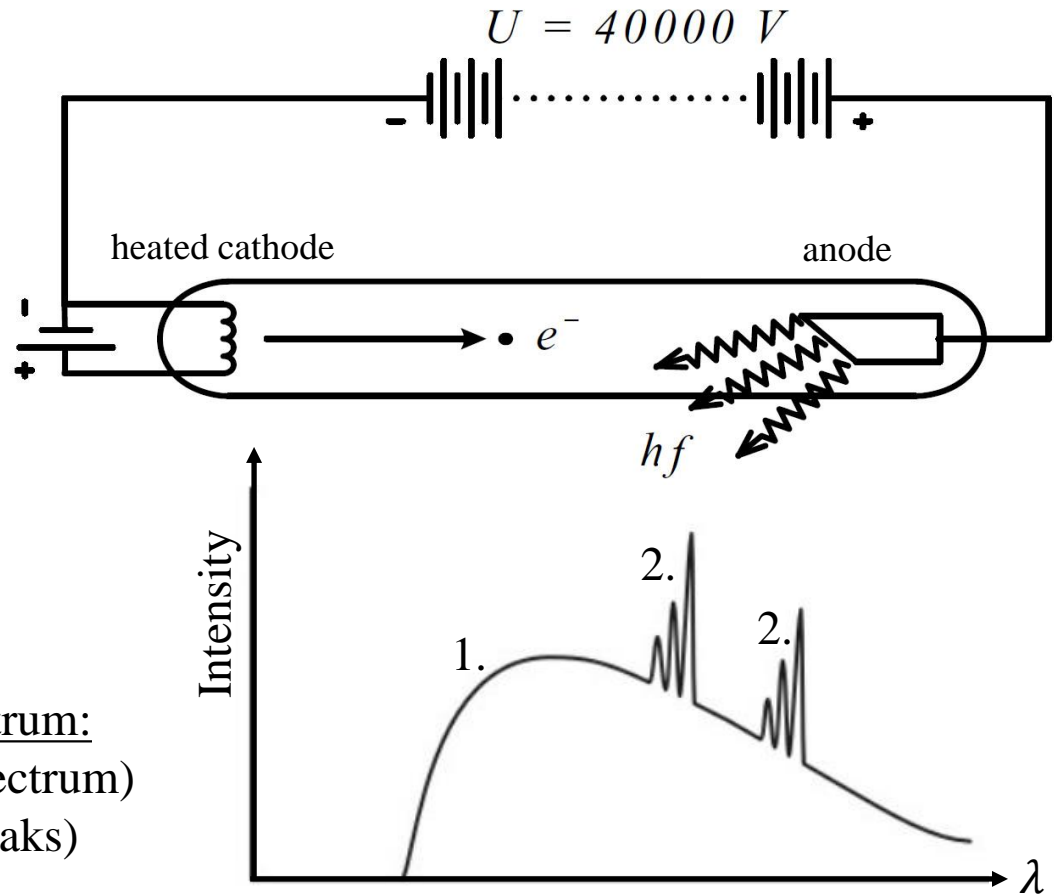
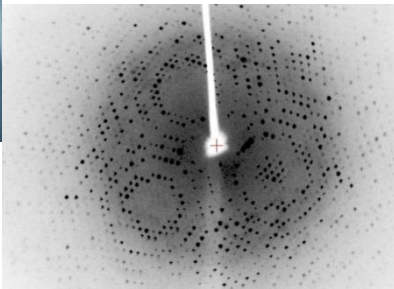
Unlike visible rays, these have great penetrating power.

Production:

- electrons emerging from a heated cathode are accelerated by high voltage
- the electrons smash into the anode, which is a metal with high atomic number (e.g. tungsten)

Main areas of use:

- medical imaging
- crystallography
- X-ray spectroscopy



Two components of the spectrum:

1. continuum (continuous spectrum)
2. characteristic radiation (peaks)

Continuum component - Bremsstrahlung (braking radiation)

Electron entering the Coulomb field of a heavy nucleus is deflected and slowed down.

Bremsstrahlung:

A charged particle (here e^-) undergoing acceleration loses energy and emits a photon.

$$E_{k1} - E_{k2} = E_f$$

$$\frac{1}{2}mv_1^2 - \frac{1}{2}mv_2^2 = hf$$

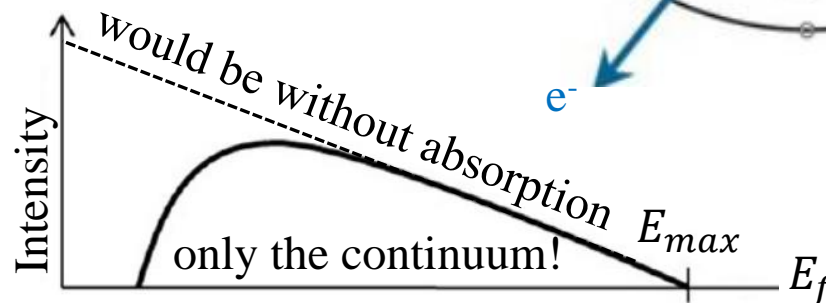
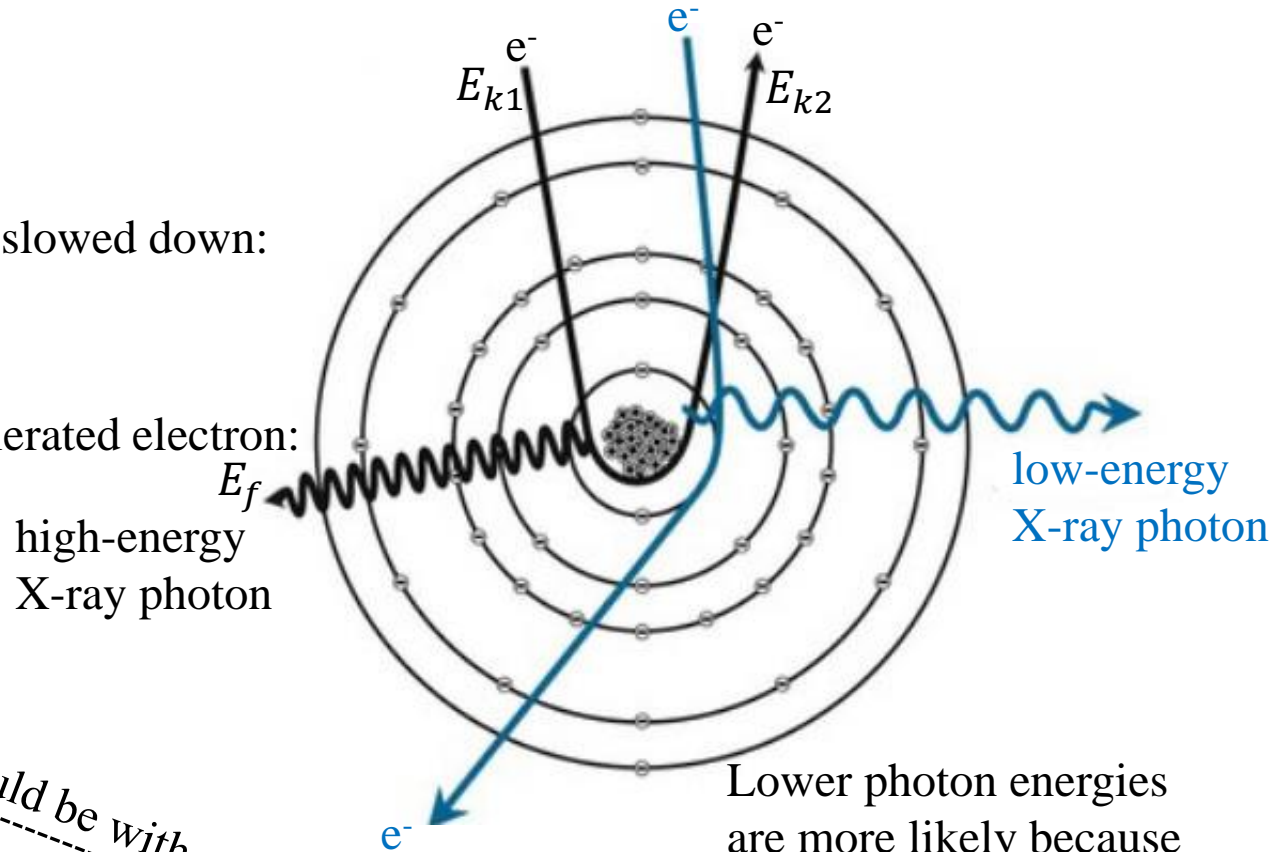
If the electron is completely slowed down:

$$\frac{1}{2}mv_1^2 = hf_{max}$$

Since the energy of the accelerated electron:

$$E_k = eU$$

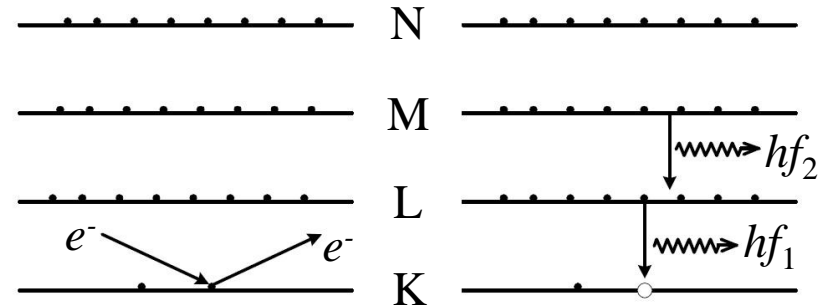
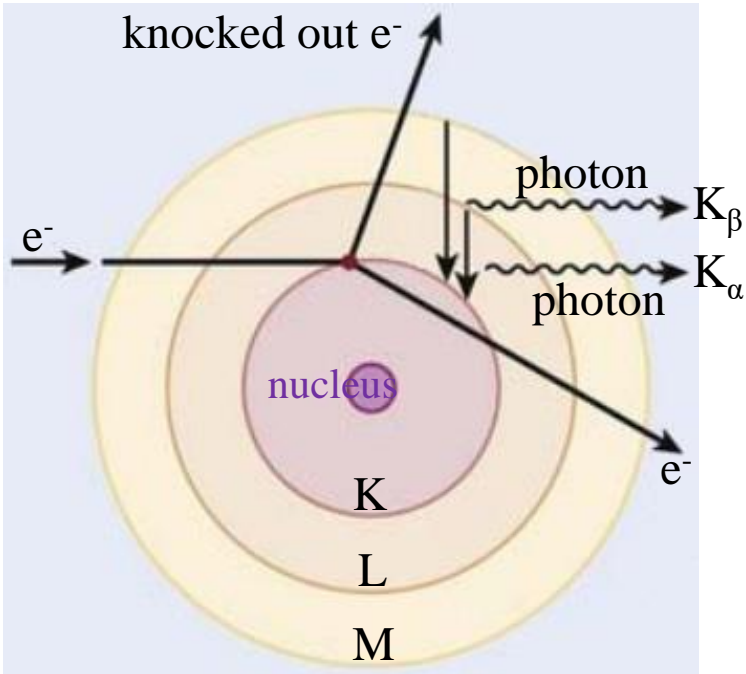
Thus, the maximum energy of the photon in eV is the accelerating voltage of the electron!



Lower photon energies are more likely because the electron can be deflected several times in the material. (straight line in the figure)

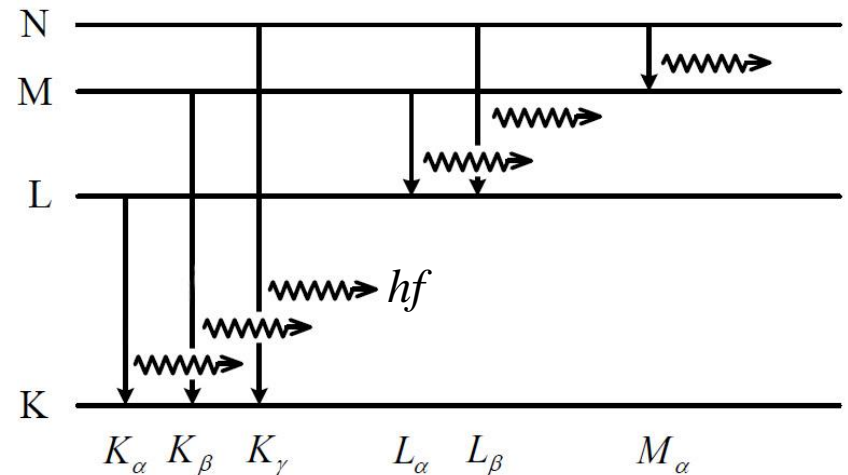
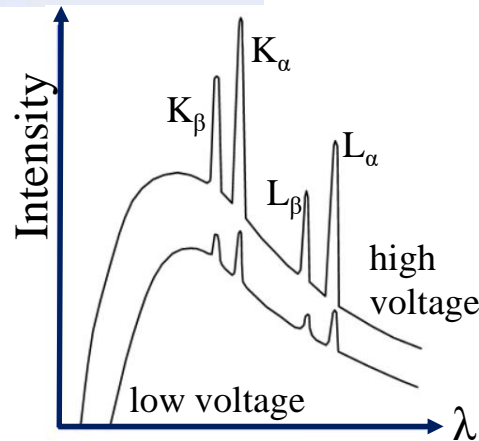
Characteristic radiation - component with lines

The accelerated electron knocks another electron out from one of the inner shells of the atom. This creates a vacancy, which causes further electron jumps.



Discrete energy photons characteristic of transition:
- lines that can be arranged in series

$$E_2 - E_1 = hf$$



Structure of the atomic nucleus

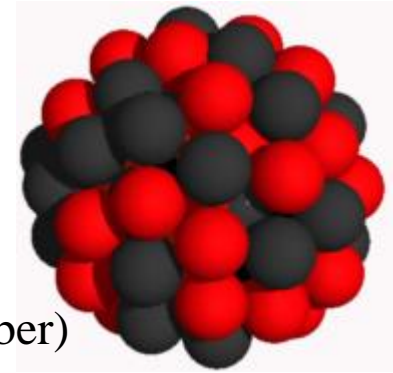
The nucleus contains positively charged protons and neutral neutrons.

Z: atomic number (number of protons, charge of nucleus in e units.)

The atomic number is also the number of electrons in a neutral atom.

A: mass number (how many times the mass of the proton or neutron)

Mass number is also the number of nucleons: $A = N + Z$ (N : neutron number)

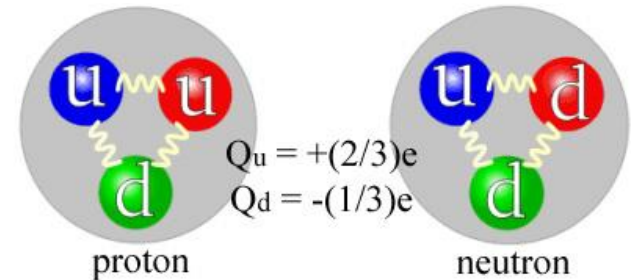
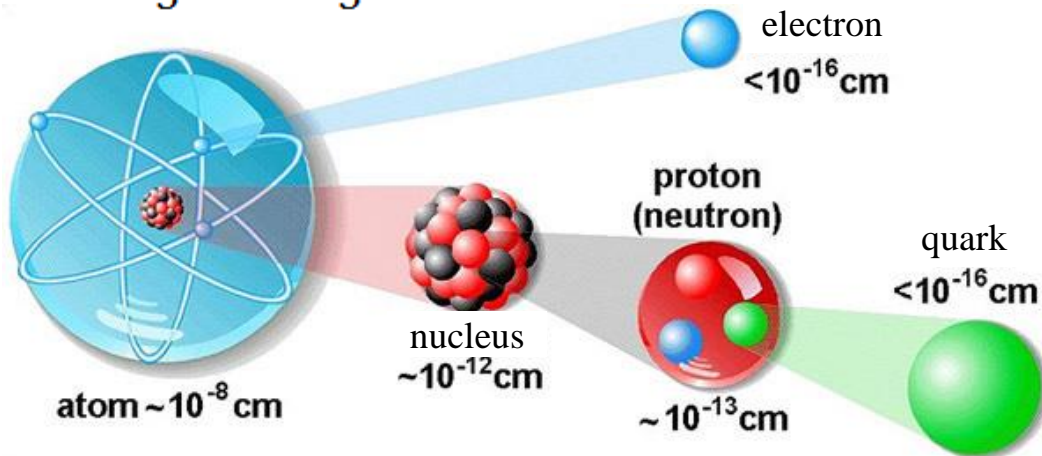


isotopes: for a given Z , N or A can be different, e.g. ${}^1_1\text{H}$, ${}^2_1\text{H}$, ${}^3_1\text{H}$ hydrogen (proton only), deuterium (proton + neutron), tritium (proton + 2 neutrons).

The density of the nucleus is independent of its size, therefore its volume is proportional to the mass number:

$$V = \frac{4R^3\pi}{3} = \frac{4R_0^3\pi}{3}A$$

so for nuclear radius: $R(A) = R_0A^{1/3}$ $R_0 = 1,4 - 1,5 \text{ fm}$



Basic building blocks and interactions

Three generations
of matter (fermions)

	I	II	III	
mass →	2.4 MeV	1.27 GeV	171.2 GeV	0
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0
spin →	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
name →	u up	c charm	t top	γ photon
	4.8 MeV	104 MeV	4.2 GeV	0
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
	d down	s strange	b bottom	g gluon
	<2.2 eV	<0.17 MeV	<15.5 MeV	91.2 GeV
	0	0	0	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	Z Z-boson
	0.511 MeV	105.7 MeV	1.777 GeV	80.4 GeV
	-1	-1	-1	± 1
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
	e electron	μ muon	τ tau	W[±] W-boson

electromagnetic

strong

weak

Bosons (particles mediating interactions)

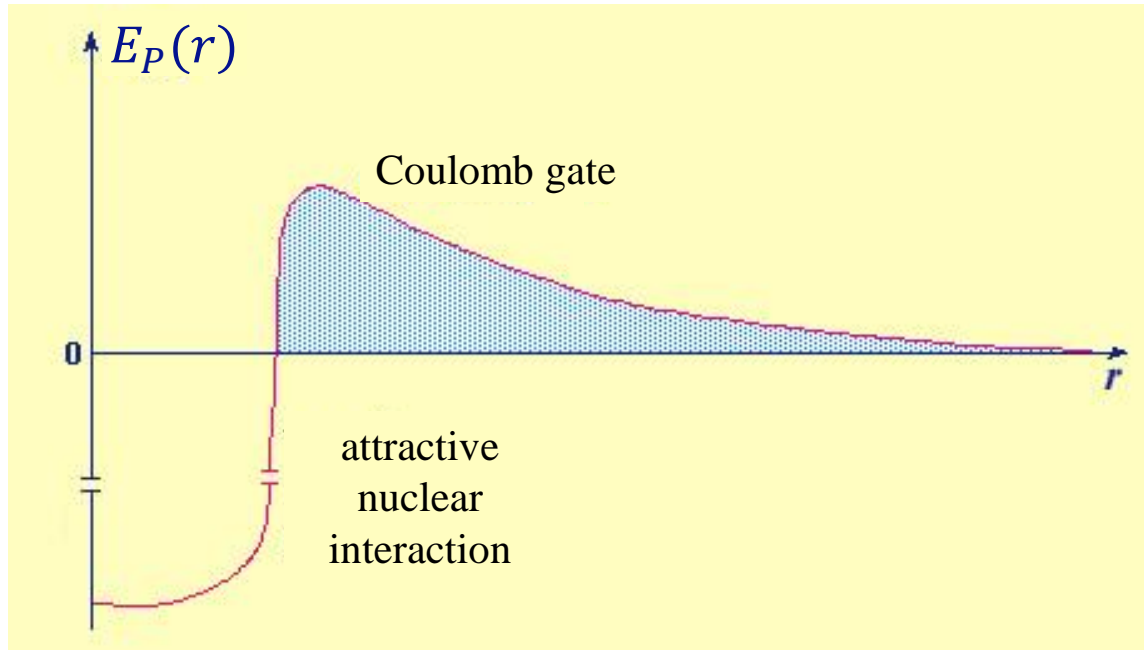
Interactions

1. electromagnetic
2. strong
3. weak
4. gravitational

Nuclear interaction

The nucleus contains Z number of protons, which repel each other due to their identical charge. However, in addition to the Coulomb interaction, a much stronger attractive force (nuclear or **strong interaction**) appears at very small distances (\sim proton radius). This is charge independent, and is attractive between p - p , p - n , and n - n .

The nucleons are therefore in a bound state, their energy is negative ($E_M = E_k + E_p$)



Quantum mechanics: protons and neutrons can only have discrete energies in the potential valley created by other nucleons, but the energies here are much higher than for electrons in the electron shell.

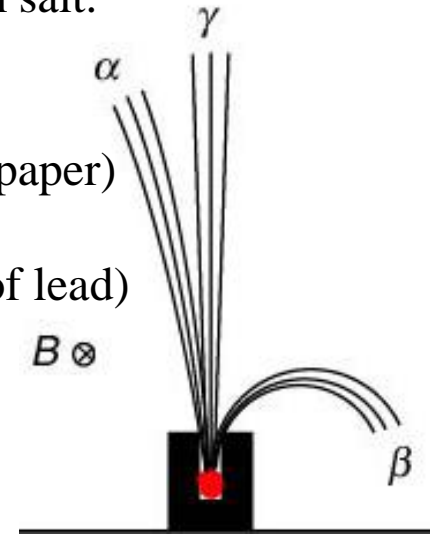
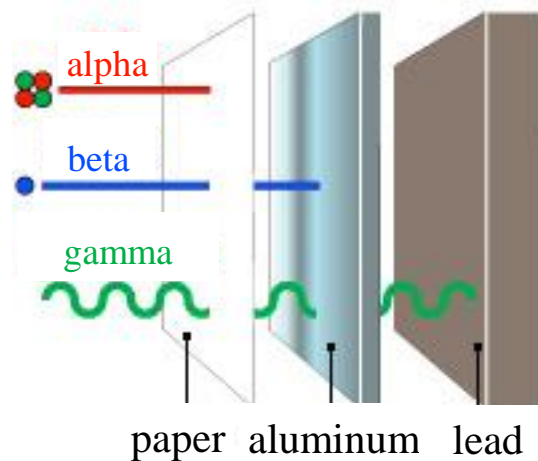
Radioactivity

Becquerel (1896): the photographic plate turns black when near uranium salt.
Later, in a magnetic field, this radiation split into three: α , β , γ .

α : helium nuclei ${}^4_2\text{He}^{2+}$ (low penetrating power, absorbed by sheet of paper)

β : electrons (near the speed of light, absorbed by a few mm Al sheet)

γ : high-energy EM radiation ($f > 10^{18}$ Hz, only absorbed by several cm of lead)

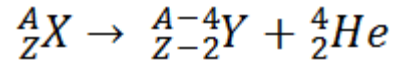


When radioactive radiation is emitted, element transmutation usually occurs (except γ).

The ejected particles are highly energetic because the nuclear forces are orders of magnitude stronger than the Coulomb force acting on electrons, so greater energies are released than during chemical reactions (electron transitions between energy levels).

Types of radioactive decay

α -decay: mass number decreases by 4, atomic number decreases by 2.



β -decay: two types (β^- and β^+) depending on whether electron (e^-) or **positron** (e^+) is created. The positron is the antiparticle of electron, with opposite charge, but everything else is same.

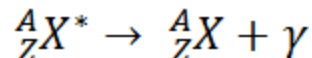


The ν and $\bar{\nu}$ represent **neutrino** and antineutrino, respectively. These are uncharged, very low-mass particles that only react through the weak interaction. This makes them extremely difficult to detect. The positron leaves the nucleus and annihilates with an electron, producing two high-energy photons (matter + antimatter).

These also include electron capture, mostly from the innermost shell:



γ -decay: does not involve element transmutation, only the transformation of the nucleus from an excited state to the ground state takes place. The energy difference is released in the form of a photon (the energy differences are large!).



Law of radioactive decay

Radioactive decay is a random phenomenon. The nucleus of a radioactive isotope decays with the same probability per unit time, regardless of its age. The laws are statistical in nature, they only hold true for large numbers.

If λ is the probability that a nucleus will decay in the next second (**decay constant**), then for the change in the number N of the nuclei (N is large!) over time dt :

Rearranging the equation (separating variables):

$$dN = -\lambda N dt \quad \frac{dN}{N} = -\lambda dt \longrightarrow \int_{N_0}^N \frac{dN}{N} = -\lambda \int_0^t dt$$

After integration: $\ln N - \ln N_0 = -\lambda t$

For the **decay law**: $N = N_0 e^{-\lambda t}$ (exponential decline, $1/\lambda$ is the average lifetime.)

The **half-life** gives the time it takes for half of the original large number of radioactive nuclei to decay. Waiting for another half-life, the number of nuclei that have not yet decayed is halved again, and so on.

$$\frac{N_0}{2} = N_0 e^{-\lambda T_{1/2}} \\ e^{\lambda T_{1/2}} = 2 \quad \longrightarrow \quad T_{1/2} = \frac{\ln 2}{\lambda}$$

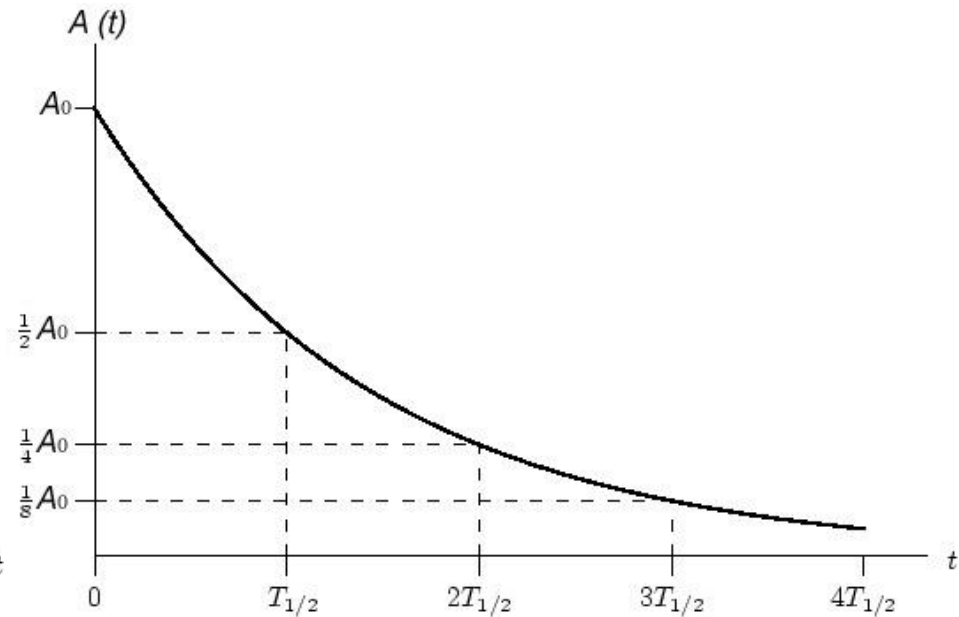
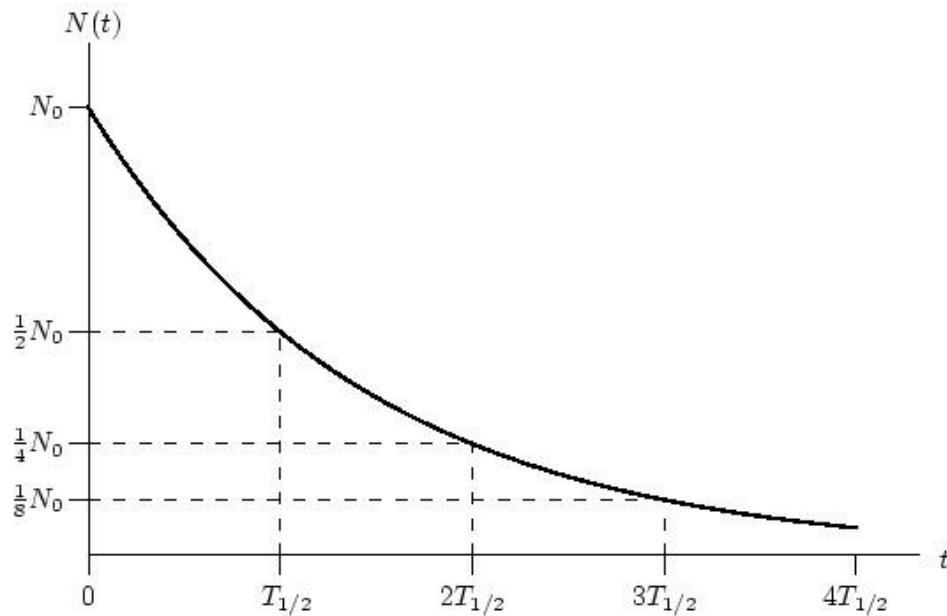
Activity

Activity: Number of decays occurring in the sample per unit time: $A = \left| \frac{dN}{dt} \right|$
[A] = 1 Bq (becquerel) = 1 decay/second

$$A = \left| \frac{dN}{dt} \right| = N_0 \lambda e^{-\lambda t} = A_0 e^{-\lambda t}$$

So the activity decreases according to the same exponential function, and at any time:

$$A(t) = N(t)\lambda$$



Mass defect

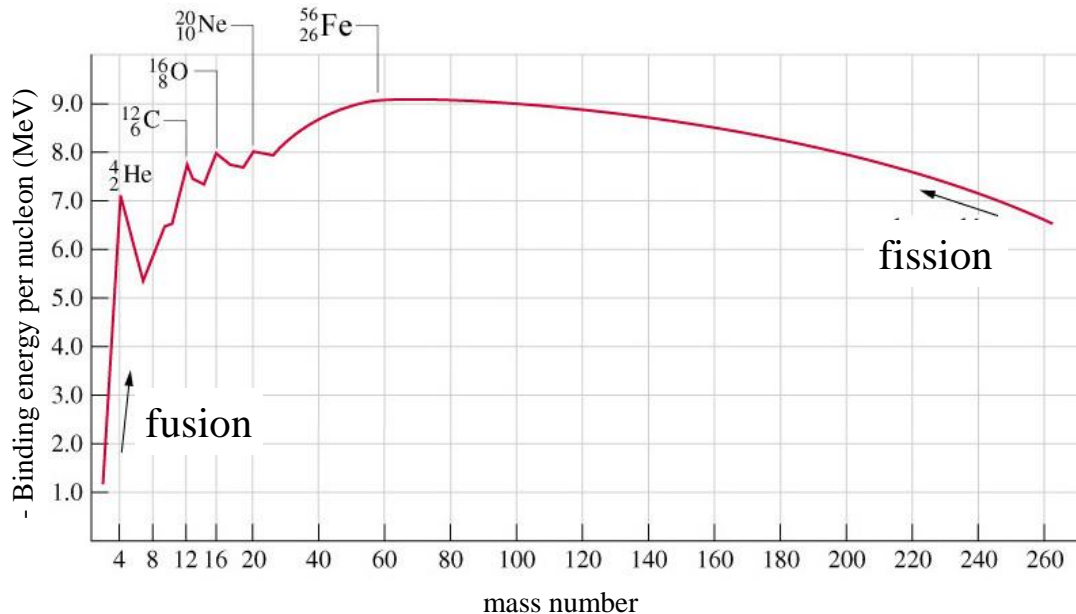
Let $M(A, Z)$ denote the mass of the nucleus with mass number A and atomic number Z . Measured with mass spectrometer, we find that the mass of the nucleus is Δm smaller than the mass of its constituents (protons and neutrons):

$$\Delta m = M(A, Z) - Zm_p - (A - Z)m_n < 0$$

This **mass defect**, calculated based on Einstein's mass-energy equivalence, gives the **binding energy** (the ~ 0 energy of free components became negative because they entered a bound state). So the binding energy gives us how much energy we would have to invest to break the nucleus (or any bound system) back into its components.

$$E_K = \Delta mc^2 < 0$$

The binding energy per nucleon can be determined by measuring the masses: $\varepsilon = E_K/A$



If ε decreases during a process, energy is released.

e.g. fusion of small nuclei
or fission of large nuclei

ε is the smallest for iron.

Nuclear power plant

If fast neutrons slow down and get captured (on average ≥ 1) \rightarrow **chain reaction**.

Uncontrolled: nuclear bomb

Critical mass: if the size of the uranium block is large enough, neutrons will slow down within it and get captured.

Controlled: **nuclear power plant**

*First self-sustaining chain reaction 1942 Chicago
Fermi and Szilárd separated natural uranium ore cells with graphite bricks (moderator).*

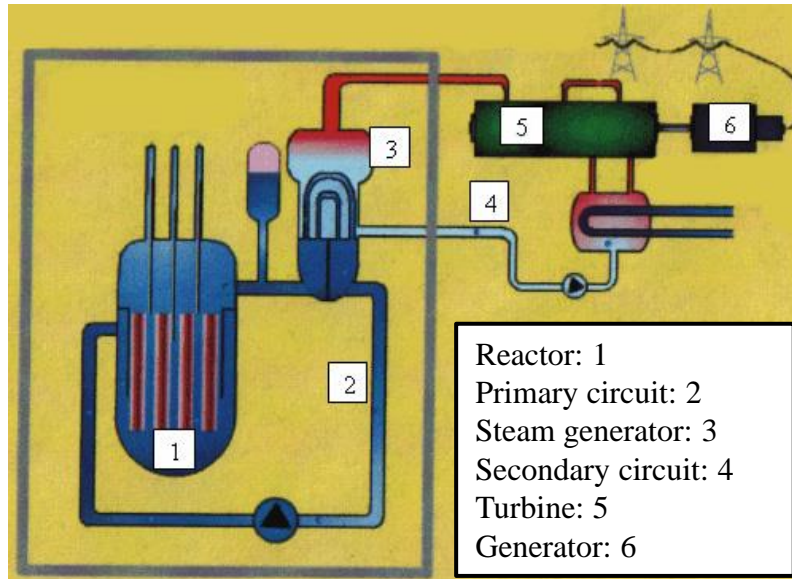
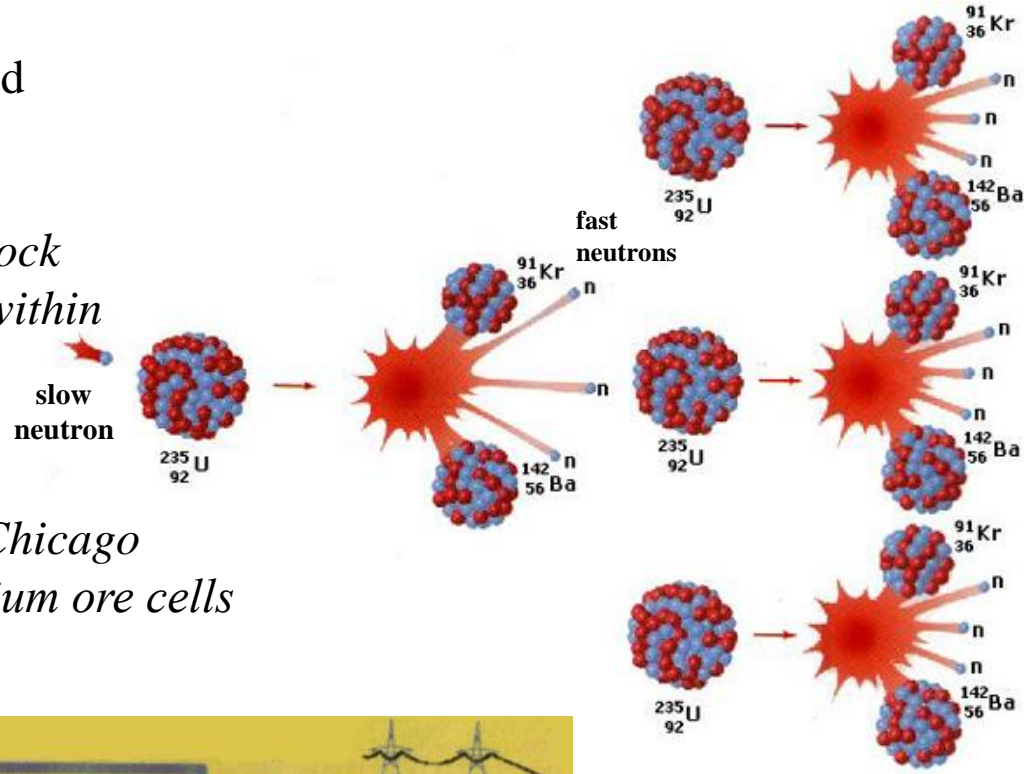
Multiplication

factor ($k = n'/n$).

n' : causes another fission

n : number of fissions

If k is kept below one, but close to it, then energy can be produced in a controlled manner.



moderator materials:

- graphite
- heavy water
- ordinary water

slowing down fast neutrons for fission.

Fusion

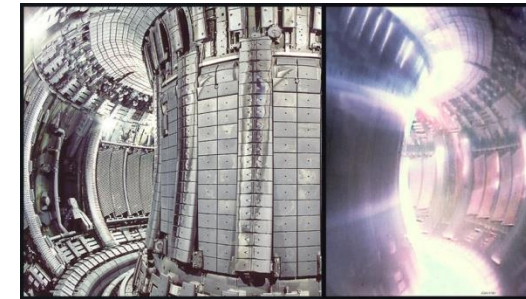
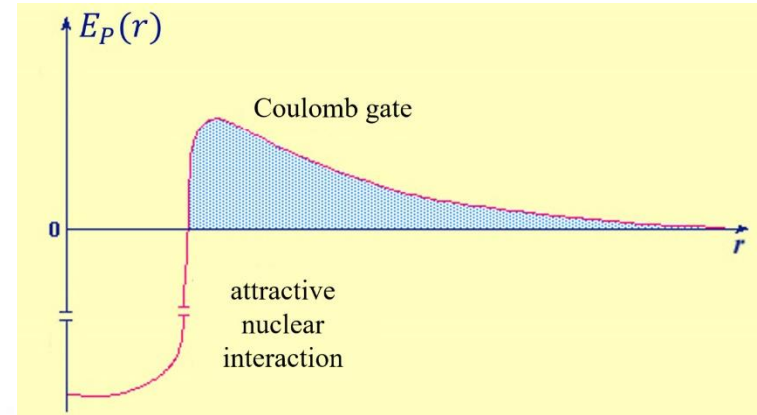
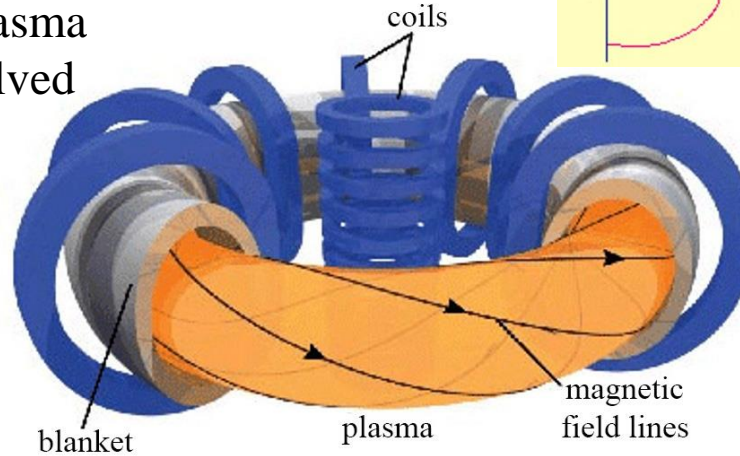
Energy is also released when smaller nuclei fuse, e.g. in the Sun or in the hydrogen bomb hydrogen is converted into helium. Problem: Due to the Coulomb barrier, temperatures of tens of millions of degrees are required for fusion between nuclei to occur.

Bomb: fission bomb heats it up

Power plant: keeping hot plasma together has not yet been solved

Two types:

1. Tokamak (held together by a magnetic bottle)



2. fusion by lasers (hydrogen in a tiny drop is ignited by focused lasers)

