

- (1) Let $f(x) = 2x - 3$ and $x_0 = 5$. Compute $f^{10}(x_0)$.
A) 2047, B) 2050, C) 2048, D) 2051, E) 2049
- (2) Compute $\begin{pmatrix} a & b \\ c & d \end{pmatrix}^{-1} = \begin{pmatrix} 1 & 0 \\ 4 & 2 \end{pmatrix}^{-1}$. How much is $a + 2b + 3c + 4d$?
A) -5, B) -6, C) -2, D) -3, E) -4
- (3) One of the eigenvectors of the matrix $\begin{pmatrix} 1 & 3 \\ 3 & 1 \end{pmatrix}$ is $\begin{pmatrix} 1 \\ -1 \end{pmatrix}$. What is the corresponding eigenvalue?
A) -2, B) -1, C) -3, D) 0, E) -4
- (4) Let $f(x) = 5x + 7$. Compute $f^{-1}(x) = cx + d$. How much is $2c + 3d$?
A) $-\frac{14}{5}$, B) $-\frac{18}{5}$, C) $-\frac{17}{5}$, D) $-\frac{16}{5}$, E) $-\frac{19}{5}$
- (5) One of the eigenvalues of the matrix $\begin{pmatrix} 1 & 4 \\ 0 & 2 \end{pmatrix}$ is 2. Compute the corresponding eigenvector $\begin{pmatrix} x \\ y \end{pmatrix}$. How much is x/y ?
A) -1, B) -4, C) -3, D) 0, E) -2
- (6) Let us take the following mapping $\phi : \begin{pmatrix} x \\ y \end{pmatrix} \rightarrow \begin{pmatrix} 2 & 3 \\ z & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$. How much is z , if ϕ is not invertible?
A) $\frac{7}{3}$, B) $\frac{2}{3}$, C) $\frac{5}{3}$, D) $\frac{4}{3}$, E) $\frac{8}{3}$

1¹: 2¹: 3¹: 4¹: 5¹: 6¹:

- (1) Compute $\begin{pmatrix} a & b \\ c & d \end{pmatrix} = \begin{pmatrix} 2 & 3 \\ 0 & 1 \end{pmatrix}^{-1}$. How much is $a + 2b + 3c + 4d$?
A) $\frac{1}{2}$, B) $\frac{5}{2}$, C) $\frac{7}{2}$, D) $-\frac{1}{2}$, E) $\frac{3}{2}$
- (2) Let us take the following mapping $\phi : \begin{pmatrix} x \\ y \end{pmatrix} \rightarrow \begin{pmatrix} 3 & z \\ 1 & 2 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$. How much is z , if ϕ is not invertible?
A) 10, B) 8, C) 9, D) 7, E) 6
- (3) Suppose that the dynamics of a two state stochastic system is generated by the matrix $\begin{pmatrix} \frac{1}{9} & \frac{9}{10} \\ \frac{1}{10} & \frac{1}{10} \end{pmatrix}$. Find the steady state probability vector $\begin{pmatrix} p_1 \\ p_2 \end{pmatrix}$. How much is p_1/p_2 ?
A) 3, B) 0, C) 1, D) 2, E) -1
- (4) One of the eigenvectors of the matrix $\begin{pmatrix} 3 & 5 \\ 5 & 3 \end{pmatrix}$ is $\begin{pmatrix} 1 \\ -1 \end{pmatrix}$. What is the corresponding eigenvalue?
A) -3, B) -4, C) -2, D) -6, E) -5
- (5) Let $f(x) = 5x + 6$. Compute $f^{-1}(x) = cx + d$. How much is $2c + 3d$?
A) $-\frac{19}{5}$, B) $-\frac{14}{5}$, C) $-\frac{17}{5}$, D) $-\frac{16}{5}$, E) $-\frac{18}{5}$
- (6) Let $f(x) = 2x - 5$ and $x_0 = 6$. Compute $f^9(x_0)$.
A) 518, B) 515, C) 519, D) 516, E) 517

1¹: 2¹: 3¹: 4¹: 5¹: 6¹:

- (1) Compute $\begin{pmatrix} a & b \\ c & d \end{pmatrix} = \begin{pmatrix} 4 & 0 \\ 2 & 1 \end{pmatrix}^{-1}$. How much is $a + 2b + 3c + 4d$?
A) $\frac{19}{4}$, B) $\frac{15}{4}$, C) $\frac{11}{4}$, D) $\frac{17}{4}$, E) $\frac{13}{4}$
- (2) One of the eigenvalues of the matrix $\begin{pmatrix} 2 & 5 \\ 0 & 4 \end{pmatrix}$ is 4. Compute the correspondig eigenvector $\begin{pmatrix} x \\ y \end{pmatrix}$. How much is x/y ?
A) $-\frac{3}{2}$, B) $\frac{1}{2}$, C) $-\frac{7}{2}$, D) $-\frac{5}{2}$, E) $-\frac{1}{2}$
- (3) One of the eigenvectors of the matrix $\begin{pmatrix} 1 & 3 \\ 3 & 1 \end{pmatrix}$ is $\begin{pmatrix} 1 \\ -1 \end{pmatrix}$. What is the corresponding eigenvalue?
A) -5 , B) -4 , C) -3 , D) -1 , E) -2
- (4) Let $f(x) = 2x - 4$ and $x_0 = 6$. Compute $f^{11}(x_0)$.
A) 4104, B) 4102, C) 4103, D) 4101, E) 4100
- (5) Let $f(x) = 2x + 3$. Compute $f^{-1}(x) = cx + d$. How much is $2c + 3d$?
A) $\frac{1}{2}$, B) $-\frac{3}{2}$, C) $-\frac{1}{2}$, D) $-\frac{7}{2}$, E) $-\frac{5}{2}$
- (6) Let us take the following mapping $\phi : \begin{pmatrix} x \\ y \end{pmatrix} \rightarrow \begin{pmatrix} 3 & z \\ 2 & 2 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$. How much is z , if ϕ is not invertible?
A) 3, B) 5, C) 7, D) 6, E) 4

1¹: 2¹: 3¹: 4¹: 5¹: 6¹:

- (1) Let $f(x) = 2x - 3$ and $x_0 = 7$. Compute $f^{10}(x_0)$.
A) 4097, B) 4101, C) 4100, D) 4099, E) 4098
- (2) Compute $\begin{pmatrix} a & b \\ c & d \end{pmatrix} = \begin{pmatrix} 2 & 0 \\ 3 & 4 \end{pmatrix}^{-1}$. How much is $a + 2b + 3c + 4d$?
A) $\frac{5}{8}$, B) $\frac{1}{8}$, C) $\frac{3}{8}$, D) $-\frac{1}{8}$, E) $-\frac{3}{8}$
- (3) Let us take the following mapping $\phi: \begin{pmatrix} x \\ y \end{pmatrix} \rightarrow \begin{pmatrix} 2 & 2 \\ 2 & 4 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$. How much is the signed area of the image of the unit square?
A) 2, B) 3, C) 5, D) 4, E) 6
- (4) One of the eigenvalues of the matrix $\begin{pmatrix} 4 & 1 \\ 0 & 7 \end{pmatrix}$ is 7. Compute the correspondig eigenvector $\begin{pmatrix} x \\ y \end{pmatrix}$. How much is x/y ?
A) $-\frac{7}{4}$, B) $-\frac{3}{4}$, C) $-\frac{1}{4}$, D) $-\frac{5}{4}$, E) $\frac{1}{4}$
- (5) Let $f(x) = 3x + 7$. Compute $f^{-1}(x) = cx + d$. How much is $2c + 3d$?
A) $-\frac{17}{3}$, B) $-\frac{14}{3}$, C) $-\frac{19}{3}$, D) $-\frac{16}{3}$, E) $-\frac{20}{3}$
- (6) One of the eigenvectors of the matrix $\begin{pmatrix} 2 & 6 \\ 6 & 2 \end{pmatrix}$ is $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$. What is the correspondig eigenvalue?
A) 4, B) 8, C) 5, D) 7, E) 6

1¹: 2¹: 3¹: 4¹: 5¹: 6¹:

- (1) One of the eigenvectors of the matrix $\begin{pmatrix} 4 & 6 \\ 6 & 4 \end{pmatrix}$ is $\begin{pmatrix} 1 \\ -1 \end{pmatrix}$. What is the corresponding eigenvalue?
A) 0, B) -1 , C) -2 , D) -3 , E) 1
- (2) Compute $\begin{pmatrix} a & b \\ c & d \end{pmatrix} = \begin{pmatrix} 4 & 0 \\ 1 & 1 \end{pmatrix}^{-1}$. How much is $a + 2b + 3c + 4d$?
A) $\frac{1}{2}$, B) $\frac{3}{2}$, C) $\frac{9}{2}$, D) $\frac{7}{2}$, E) $\frac{5}{2}$
- (3) Let us take the following mapping $\phi: \begin{pmatrix} x \\ y \end{pmatrix} \rightarrow \begin{pmatrix} 4 & z \\ 4 & 2 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$. How much is z , if ϕ is not invertible?
A) 2 , B) 3 , C) 4 , D) 1 , E) 0
- (4) Let $f(x) = 3x + 5$. Compute $f^{-1}(x) = cx + d$. How much is $2c + 3d$?
A) $-\frac{16}{3}$, B) $-\frac{11}{3}$, C) $-\frac{17}{3}$, D) $-\frac{13}{3}$, E) $-\frac{14}{3}$
- (5) Let $f(x) = 2x - 3$ and $x_0 = 6$. Compute $f^9(x_0)$.
A) 1538 , B) 1542 , C) 1540 , D) 1539 , E) 1541
- (6) One of the eigenvalues of the matrix $\begin{pmatrix} 1 & 3 \\ 0 & 5 \end{pmatrix}$ is 5 . Compute the corresponding eigenvector $\begin{pmatrix} x \\ y \end{pmatrix}$. How much is x/y ?
A) -6 , B) -3 , C) -5 , D) -4 , E) -7

1¹: 2¹: 3¹: 4¹: 5¹: 6¹:

- (1) Let $f(x) = 2x + 3$. Compute $f^{-1}(x) = cx + d$. How much is $2c + 3d$?
 A) $\frac{1}{2}$, B) $-\frac{3}{2}$, C) $-\frac{1}{2}$, D) $-\frac{5}{2}$, E) $-\frac{7}{2}$
- (2) Compute $\begin{pmatrix} a & b \\ c & d \end{pmatrix} = \begin{pmatrix} 3 & 0 \\ 4 & 4 \end{pmatrix}^{-1}$. How much is $a + 2b + 3c + 4d$?
 A) $\frac{4}{3}$, B) $-\frac{1}{3}$, C) $\frac{1}{3}$, D) $\frac{2}{3}$, E) $\frac{5}{3}$
- (3) Let $f(x) = 2x - 2$ and $x_0 = 4$. Compute $f^{10}(x_0)$.
 A) 2047, B) 2050, C) 2049, D) 2048, E) 2051
- (4) One of the eigenvectors of the matrix $\begin{pmatrix} 1 & 5 \\ 5 & 1 \end{pmatrix}$ is $\begin{pmatrix} 1 \\ -1 \end{pmatrix}$. What is the corresponding eigenvalue?
 A) -4, B) -1, C) 0, D) -3, E) -2
- (5) Let us take the following mapping $\phi : \begin{pmatrix} x \\ y \end{pmatrix} \rightarrow \begin{pmatrix} 2 & 2 \\ 4 & 4 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$. How much is the signed area of the image of the unit square?
 A) -2, B) -3, C) -1, D) -4, E) 0
- (6) Suppose that the dynamics of a two state stochastic system is generated by the matrix $\begin{pmatrix} \frac{1}{2} & \frac{3}{5} \\ \frac{1}{2} & \frac{2}{5} \end{pmatrix}$. Find the steady state probability vector $\begin{pmatrix} p_1 \\ p_2 \end{pmatrix}$. How much is p_1/p_2 ?
 A) $\frac{7}{5}$, B) $\frac{11}{5}$, C) $\frac{9}{5}$, D) $\frac{6}{5}$, E) $\frac{8}{5}$

1¹: 2¹: 3¹: 4¹: 5¹: 6¹:

- 1** 1: D¹, 2: D¹, 3: A¹, 4: E¹, 5: B¹, 6: B¹,
2 1: E¹, 2: E¹, 3: C¹, 4: C¹, 5: D¹, 6: E¹,
3 1: C¹, 2: D¹, 3: E¹, 4: E¹, 5: D¹, 6: A¹,
4 1: D¹, 2: C¹, 3: D¹, 4: C¹, 5: C¹, 6: B¹,
5 1: C¹, 2: D¹, 3: A¹, 4: D¹, 5: D¹, 6: B¹,

6 1: E¹, 2: C¹, 3: B¹, 4: A¹, 5: E¹, 6: D¹,