

1. FELADATSOR 1, MATEMATIKA I.

1.1.

- (1) Legyen $u = 3 + 3i$, $v = 1 + i$. Mennyi uv ?
 A) $1 + 4i$, B) $-2 + 7i$, C) $2 + 4i$, D) $-1 + 8i$, E) $6i$
 E
- (2) Legyen $u = 4 + 2i$, $v = 3 + 4i$. Mennyi u/v ?
 A) $1 - \frac{4i}{5}$, B) $\frac{4}{5} - \frac{2i}{5}$, C) $1 - \frac{3i}{5}$, D) $\frac{3}{5}$, E) $\frac{2}{5} - \frac{4i}{5}$
 B
- (3) Legyen $u = 3 + 2i$, $v = 2 + 2i$. Mennyi $uv - i\bar{v} + u\bar{u}$?
 A) $13 + 8i$, B) $12 + 6i$, C) $15 + 7i$, D) $11 + 7i$, E) $11 + 9i$
 A
- (4)

$$(-1 - i)u + (-1 - i)v = 2i$$

$$(1 + i)u + (-1 + i)v = 2 - 2i$$
 Mennyi $u + v$?
 A) 2, B) 0, C) $-2i$, D) $2i$, E) $-1 - i$
 E
- (5) Legyen $-3 - i + (-3 + 3i)z = 1 - i$. Mennyi z
 A) $-\frac{4}{3}$, B) $-\frac{2}{3} - \frac{2i}{3}$, C) $-\frac{i}{3}$, D) 0, E) $-\frac{1}{3} - \frac{i}{3}$
 B
- (6) Legyen $z = (-4 + 4i)\sqrt{2}$. Mennyi $\operatorname{Arg}(z)$ es $|z|$?
 A) $\{\frac{\pi}{4}, 1\}$, B) $\{\frac{\pi}{4}, 2\}$, C) $\{\frac{\pi}{4}, 2\sqrt{2}\}$, D) $\{\frac{\pi}{4}, \sqrt{2}\}$, E) $\{\frac{3\pi}{4}, 8\}$
 E
- (7) Legyen $z = 4 - 4i$. Mennyi $\operatorname{Arg}(z)$ es $|z|$?
 A) $\{45^\circ, 1\}$, B) $\{45^\circ, \sqrt{2}\}$, C) $\{45^\circ, 2\sqrt{2}\}$, D) $\{-45^\circ, 4\sqrt{2}\}$, E) $\{45^\circ, 2\}$
 D
- (8) Legyen $z = 1 - i\sqrt{3}$. Mennyi $\operatorname{Arg}(z)$ es $|z|$?
 A) $\{\frac{2\pi}{3}, 2\}$, B) $\{\frac{2\pi}{3}, 3\}$, C) $\{\frac{\pi}{6}, 2\}$, D) $\{\frac{\pi}{6}, 3\}$, E) $\{-\frac{\pi}{3}, 2\}$
 E
- (9) Legyen $z = 1 - i\sqrt{3}$. Mennyi $\operatorname{Arg}(z)$ es $|z|$?
 A) $\{-60^\circ, 2\}$, B) $\{120^\circ, 2\}$, C) $\{30^\circ, 2\}$, D) $\{120^\circ, 3\}$, E) $\{30^\circ, 3\}$
 A
- (10) Mennyi a $(2x^2 + 4x + 2) : (x + 3)$ osztas hanyadosa es maradeka?
 A) $\{2x - 3, 6\}$, B) $\{2x + 1, 10\}$, C) $\{2x - 2, 8\}$, D) $\{2x + 1, 7\}$, E) $\{2x - 3, 9\}$
 C
- (11) Legyen $\frac{4}{x^2 - 25} = \frac{A}{x-a} + \frac{B}{x-b}$ Mennyi lehet (A, B) ?
 A) $\{0, 0\}$, B) $\{\frac{1}{5}, -\frac{1}{5}\}$, C) $\{\frac{2}{5}, -\frac{2}{5}\}$, D) $\{-\frac{2}{5}, \frac{2}{5}\}$, E) $\{-\frac{1}{5}, \frac{1}{5}\}$
 C

- (12) Legyen $\frac{3}{x^2-25x} = \frac{A}{x-a} + \frac{B}{x-b}$ Mennyi lehet A, B
 A) $\left\{\frac{3}{25}, -\frac{3}{25}\right\}$, B) $\left\{\frac{1}{25}, -\frac{1}{5}\right\}$, C) $\left\{\frac{2}{25}, -\frac{4}{25}\right\}$, D) $\left\{0, -\frac{6}{25}\right\}$, E) $\left\{\frac{3}{25}, -\frac{3}{25}\right\}$
 E
- (13) Legyen $\frac{(4x+3)}{x^2-25} = \frac{A}{x-a} + \frac{B}{x-b}$ Mennyi lehet (A, B)
 A) $\left\{\frac{19}{10}, \frac{13}{10}\right\}$, B) $\left\{2, \frac{7}{5}\right\}$, C) $\left\{\frac{11}{5}, \frac{8}{5}\right\}$, D) $\left\{\frac{23}{10}, \frac{17}{10}\right\}$, E) $\left\{\frac{21}{10}, \frac{3}{2}\right\}$
 D
- (14) Melyek a $p(x) = 7x^2 + 7$ polinom gyohei?
 A) $\{1, 0\}$, B) $\{-i, -i\}$, C) $\{-i, i\}$, D) $\{1, -1\}$, E) $\{-i, 0\}$
 C
- (15) Melyek a $p(x) = 9x^2 + 9x$ polinom gyohei?
 A) $\{-i, -i\}$, B) $\{-1, 1\}$, C) $\{-1, 0\}$, D) $\{-1, -1\}$, E) $\{-i, 0\}$
 C
- (16) Legyen $z = -1 - i$. Mennyi z^4 algebrai alakja?
 A) $-4i$, B) 4 , C) -4 , D) $4i$, E) $8i$
 C
- (17) Legyen $z = -1 - i$. Mennyi z^4 hossza es szoge?
 A) $\{4, 0\}$, B) $\{4, -\frac{\pi}{2}\}$, C) $\{4, \frac{\pi}{2}\}$, D) $\{8, \frac{\pi}{2}\}$, E) $\{4, \pi\}$
 E
- (18) Legyen $z = -1 + i$. Mennyi z^5 hossza es szoge?
 A) $\{4\sqrt{2}, -135^\circ\}$, B) $\{8\sqrt{2}, -135^\circ\}$, C) $\{4\sqrt{2}, -45^\circ\}$, D) $\{4\sqrt{2}, 135^\circ\}$, E) $\{4\sqrt{2}, 45^\circ\}$
 C
- (19) Legyen $\bar{a} = \{3, 2, 3\}$, $\bar{b} = \{3, 2, 3\}$. Mekkora az \bar{a} es a \bar{b} ? vektorok altal kifeszitett haromszog terulete?
 A) 0, B) 0, C) 22, D) 0, E) 22
 A
- (20) Legyen $z = 1 - i\sqrt{3}$. Mennyi z^4 hossza es szoge?
 A) $\{16, -60^\circ\}$, B) $\{16, 30^\circ\}$, C) $\{32, 30^\circ\}$, D) $\{16, 120^\circ\}$, E) $\{16, -150^\circ\}$
 D
- (21) Legyen $z = -\sqrt{3} - i$. Mennyi z^4 hossza es szoge?
 A) $\{16, \frac{\pi}{6}\}$, B) $\{16, \frac{2\pi}{3}\}$, C) $\{16, -\frac{\pi}{3}\}$, D) $\{16, -\frac{5\pi}{6}\}$, E) $\{32, \frac{\pi}{6}\}$
 B
- (22) Legyen $\bar{a} = \{1, 3, 1\}$, $\bar{b} = \{3, 2, 3\}$. Mennyi $\bar{a}\bar{b}$?
 A) $\{7, 0, -7\}$, B) $\{3, 6, 3\}$, C) 12, D) 11, E) $\{4, 5, 4\}$
 C
- (23) Legyen $\bar{a} = \{1, 3, 3\}$, $\bar{b} = \{2, 1, 1\}$. Mennyi $\bar{a} \times \bar{b}$?
 A) 0, B) 8, C) $\{0, -5, -5\}$, D) $\{0, 5, -5\}$, E) $\{2, 3, 3\}$
 D
- (24) Legyen $\bar{a} = \{3, 1, 2\}$, $\bar{b} = \{2, 3, 1\}$, $\bar{c} = \{1, 1, 2\}$. Mennyi $\bar{a}\bar{b}\bar{c}$?
 A) 9, B) 10, C) 10, D) 7, E) 8
 B

(25) Legyen $\bar{a} = \{1, 3, 3\}$. Mennyi \bar{a} hossza?

A) 19, B) $\sqrt{7}$, C) 1, D) 7, E) $\sqrt{19}$

E

(26) Legyen $\bar{a} = \{2, 3, 1\}$, $\bar{b} = \{2, 2, 1\}$. Mennyi az \bar{a} es \bar{b} vektorok kozotti szög koszinuszsa?

A) $\frac{11}{3\sqrt{14}}$, B) $\frac{11}{30}$, C) $\frac{\sqrt{14}}{3}$, D) $\frac{3\sqrt{14}}{11}$, E) $\frac{11}{126}$

A

(27) Legyen $\bar{a} = \{1, 1, 2\}$. Mennyi x , ha \bar{a} es $\{1, x, 3\}$ megoleges egymásra?

A) -9, B) -7, C) -7, D) -10, E) -8

B

(28) Legyen $\bar{u} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$, $\bar{v} = \begin{pmatrix} 3 \\ 0 \end{pmatrix}$. Mennyi $\begin{pmatrix} p \\ q \end{pmatrix}$, ha $p\bar{u} + q\bar{v} = \begin{pmatrix} 2 \\ 2 \end{pmatrix}$?

A) $\begin{pmatrix} 2 \\ 0 \end{pmatrix}$, B) $\begin{pmatrix} 1 \\ -1 \end{pmatrix}$, C) $\begin{pmatrix} -1 \\ -3 \end{pmatrix}$, D) $\begin{pmatrix} 0 \\ -2 \end{pmatrix}$, E) $\begin{pmatrix} 2 \\ 0 \end{pmatrix}$

A

(29) Legyen $\bar{u} = \begin{pmatrix} 3 \\ 3 \end{pmatrix}$, $\bar{v} = \begin{pmatrix} 3 \\ 0 \end{pmatrix}$. Mennyi $\begin{pmatrix} p \\ q \end{pmatrix}$, ha $p\bar{u} + q\bar{v} = \begin{pmatrix} x \\ y \end{pmatrix}$?

A) $\begin{pmatrix} \frac{y}{3} \\ \frac{x}{3} - \frac{y}{3} \end{pmatrix}$, B) $\begin{pmatrix} \frac{y}{3} - 2x \\ -\frac{5x}{3} - \frac{y}{3} \end{pmatrix}$, C) $\begin{pmatrix} \frac{y}{3} - 3x \\ -\frac{8x}{3} - \frac{y}{3} \end{pmatrix}$, D) $\begin{pmatrix} \frac{y}{3} \\ \frac{x}{3} - \frac{y}{3} \end{pmatrix}$, E) $\begin{pmatrix} \frac{y}{3} - x \\ -\frac{2x}{3} - \frac{y}{3} \end{pmatrix}$

D

1.2.

- (1) Legyen $u = 3 + 2i$, $v = 2 + 2i$. Mennyi uv ?
 A) $9i$, B) $1 + 9i$, C) $1 + 8i$, D) $2 + 10i$, E) $1 + 11i$
 D
- (2) Legyen $u = 1 + 4i$, $v = 4 + i$. Mennyi u/v ?
 A) $\frac{6}{17} + \frac{14i}{17}$, B) $\frac{6}{17} + \frac{13i}{17}$, C) $\frac{9}{17} + \frac{14i}{17}$, D) $\frac{8}{17} + \frac{15i}{17}$, E) $\frac{6}{17} + \frac{16i}{17}$
 D
- (3) Legyen $u = 4 + 4i$, $v = 1 + i$. Mennyi $uv - i\bar{v} + u\bar{u}$?
 A) $33 + 8i$, B) $32 + 9i$, C) $30 + 6i$, D) $31 + 7i$, E) $29 + 9i$
 D
- (4) $(1+i)u + (1+i)v = -2i$
 $(-1-i)u + (1+i)v = -2$
 Mennyi $u + v$?
 A) 2 , B) $-1 - i$, C) $-2i$, D) 0 , E) $2i$
 B
- (5) Legyen $3 + 3i + (3 + 2i)z = -2 - i$. Mennyi z ?
 A) $-\frac{21}{13} - \frac{4i}{13}$, B) $-\frac{22}{13} - \frac{3i}{13}$, C) $-\frac{24}{13}$, D) $-\frac{23}{13} - \frac{2i}{13}$, E) $-\frac{25}{13} - \frac{i}{13}$
 D
- (6) Legyen $z = 2 - 2i$. Mennyi $\operatorname{Arg}(z)$ es $|z|$?
 A) $\{\frac{\pi}{4}, \sqrt{2}\}$, B) $\{\frac{\pi}{4}, 2\}$, C) $\{-\frac{\pi}{4}, 2\sqrt{2}\}$, D) $\{\frac{\pi}{4}, 2\sqrt{2}\}$, E) $\{\frac{\pi}{4}, 1\}$
 C
- (7) Legyen $z = 4 + 4i$. Mennyi $\operatorname{Arg}(z)$ es $|z|$?
 A) $\{45^\circ, 4\sqrt{2}\}$, B) $\{45^\circ, 2\sqrt{2}\}$, C) $\{45^\circ, \sqrt{2}\}$, D) $\{45^\circ, 2\}$, E) $\{45^\circ, 1\}$
 A
- (8) Legyen $z = \sqrt{3} - i$. Mennyi $\operatorname{Arg}(z)$ es $|z|$?
 A) $\{\frac{\pi}{6}, 2\}$, B) $\{\frac{\pi}{6}, 3\}$, C) $\{\frac{2\pi}{3}, 3\}$, D) $\{-\frac{\pi}{6}, 2\}$, E) $\{\frac{2\pi}{3}, 2\}$
 D
- (9) Legyen $z = -1 - i\sqrt{3}$. Mennyi $\operatorname{Arg}(z)$ es $|z|$?
 A) $\{30^\circ, 2\}$, B) $\{120^\circ, 2\}$, C) $\{30^\circ, 3\}$, D) $\{120^\circ, 3\}$, E) $\{-120^\circ, 2\}$
 E
- (10) Mennyi a $(x^2 + 4x + 4) : (x + 2)$ osztas hanyadosa es maradeka?
 A) $\{x + 4, -1\}$, B) $\{x + 2, 0\}$, C) $\{x + 3, 3\}$, D) $\{x, -1\}$, E) $\{x + 6, 1\}$
 B
- (11) Legyen $\frac{2}{x^2 - 9} = \frac{A}{x-a} + \frac{B}{x-b}$ Mennyi lehet (A, B) ?
 A) $\{-\frac{1}{3}, \frac{1}{3}\}$, B) $\{\frac{1}{3}, -\frac{1}{3}\}$, C) $\{\frac{2}{3}, -\frac{2}{3}\}$, D) $\{0, 0\}$, E) $\{\frac{1}{3}, -\frac{1}{3}\}$
 E
- (12) Legyen $\frac{4}{x^2 - 25x} = \frac{A}{x-a} + \frac{B}{x-b}$ Mennyi lehet A, B ?
 A) $\{0, -\frac{8}{25}\}$, B) $\{\frac{1}{25}, -\frac{7}{25}\}$, C) $\{\frac{2}{25}, -\frac{6}{25}\}$, D) $\{\frac{3}{25}, -\frac{1}{5}\}$, E) $\{\frac{4}{25}, -\frac{4}{25}\}$
 E

- (13) Legyen $\frac{3x+2}{x^2-25} = \frac{A}{x-a} + \frac{B}{x-b}$ Mennyi lehet (A, B)
 A) $\left\{\frac{17}{10}, \frac{13}{10}\right\}$, B) $\left\{\frac{7}{5}, 1\right\}$, C) $\left\{\frac{3}{2}, \frac{11}{10}\right\}$, D) $\left\{\frac{17}{10}, \frac{13}{10}\right\}$, E) $\left\{\frac{8}{5}, \frac{6}{5}\right\}$
 A

- (14) Melyek a $p(x) = 3x^2 + 5$ polinom gyökei?
 A) $\left\{-i\sqrt{\frac{5}{3}}, 0\right\}$, B) $\left\{\sqrt{\frac{5}{3}}, 0\right\}$, C) $\left\{\sqrt{\frac{5}{3}}, -\sqrt{\frac{5}{3}}\right\}$, D) $\left\{-i\sqrt{\frac{5}{3}}, -i\sqrt{\frac{5}{3}}\right\}$, E) $\left\{-i\sqrt{\frac{5}{3}}, i\sqrt{\frac{5}{3}}\right\}$
 E

- (15) Melyek a $p(x) = 8x^2 + 2x$ polinom gyökei?
 A) $\left\{-\frac{1}{4}, -\frac{1}{4}\right\}$, B) $\left\{-\frac{i}{4}, -\frac{i}{4}\right\}$, C) $\left\{-\frac{1}{4}, 0\right\}$, D) $\left\{-\frac{1}{4}, \frac{1}{4}\right\}$, E) $\left\{-\frac{i}{4}, 0\right\}$
 C

- (16) Legyen $z = 1 + i$. Mennyi z^6 algebrai alakja?
 A) -16 , B) 8 , C) $-8i$, D) -8 , E) $8i$
 C

- (17) Legyen $z = -1 + i$. Mennyi z^3 hossza és szöge?
 A) $\{2\sqrt{2}, -\frac{3\pi}{4}\}$, B) $\{4\sqrt{2}, -\frac{\pi}{4}\}$, C) $\{2\sqrt{2}, -\frac{\pi}{4}\}$, D) $\{2\sqrt{2}, \frac{\pi}{4}\}$, E) $\{2\sqrt{2}, \frac{3\pi}{4}\}$
 D

- (18) Legyen $z = -1 + i$. Mennyi z^4 hossza és szöge?
 A) $\{4, 90^\circ\}$, B) $\{4, -90^\circ\}$, C) $\{4, 0\}$, D) $\{4, 180^\circ\}$, E) $\{8, 90^\circ\}$
 D

- (19) Legyen $\bar{a} = \{2, 1, 3\}$, $\bar{b} = \{2, 1, 3\}$. Mekkora az \bar{a} és a \bar{b} vektorok által kifeszített háromszög területe?
 A) 0 , B) 0 , C) 0 , D) 14 , E) 14
 A

- (20) Legyen $z = -1 + i\sqrt{3}$. Mennyi z^2 hossza és szöge?
 A) $\{4, -30^\circ\}$, B) $\{8, 150^\circ\}$, C) $\{4, 150^\circ\}$, D) $\{4, 60^\circ\}$, E) $\{4, -120^\circ\}$
 E

- (21) Legyen $z = \sqrt{3} + i$. Mennyi z^2 hossza és szöge?
 A) $\{4, -\frac{\pi}{6}\}$, B) $\{8, -\frac{\pi}{6}\}$, C) $\{4, \frac{5\pi}{6}\}$, D) $\{4, \frac{\pi}{3}\}$, E) $\{4, -\frac{2\pi}{3}\}$
 D

- (22) Legyen $\bar{a} = \{2, 2, 3\}$, $\bar{b} = \{3, 2, 3\}$. Mennyi $\bar{a}\bar{b}$?
 A) $\{6, 4, 9\}$, B) 19 , C) 17 , D) $\{5, 4, 6\}$, E) $\{0, 3, -2\}$
 B

- (23) Legyen $\bar{a} = \{3, 3, 1\}$, $\bar{b} = \{3, 3, 3\}$. Mennyi $\bar{a} \times \bar{b}$?
 A) 0 , B) $\{9, 9, 3\}$, C) $\{6, 6, 0\}$, D) 21 , E) $\{6, -6, 0\}$
 E

- (24) Legyen $\bar{a} = \{1, 1, 1\}$, $\bar{b} = \{1, 1, 2\}$, $\bar{c} = \{3, 3, 3\}$. Mennyi $\bar{a}\bar{b}\bar{c}$?
 A) -1 , B) -3 , C) 0 , D) 0 , E) -2
 C

- (25) Legyen $\bar{a} = \{2, 1, 2\}$. Mennyi \bar{a} hossza?
 A) $\sqrt{5}$, B) $\sqrt{2}$, C) 3 , D) 5 , E) 9
 C

(26) Legyen $\bar{a} = \{3, 1, 3\}$, $\bar{b} = \{1, 1, 3\}$. Mennyi az \bar{a} és \bar{b} vektorok kozotti szög koszinusza?

A) $\frac{13}{209}$, B) $\sqrt{\frac{19}{11}}$, C) $\frac{13}{35}$, D) $\frac{\sqrt{209}}{13}$, E) $\frac{13}{\sqrt{209}}$

E

(27) Legyen $\bar{a} = \{3, 1, 1\}$. Mennyi x , ha \bar{a} es $\{1, x, 3\}$ megoleges egymásra?

A) -7, B) -6, C) -9, D) -8, E) -6

B

(28) Legyen $\bar{u} = \begin{pmatrix} 2 \\ 4 \end{pmatrix}$, $\bar{v} = \begin{pmatrix} 0 \\ 3 \end{pmatrix}$. Mennyi $\begin{pmatrix} p \\ q \end{pmatrix}$, ha $p\bar{u} + q\bar{v} = \begin{pmatrix} 2 \\ 4 \end{pmatrix}$?

A) $\begin{pmatrix} 0 \\ -1 \end{pmatrix}$, B) $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$, C) $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$, D) $\begin{pmatrix} -1 \\ -2 \end{pmatrix}$, E) $\begin{pmatrix} -2 \\ -3 \end{pmatrix}$

C

(29) Legyen $\bar{u} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$, $\bar{v} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$. Mennyi $\begin{pmatrix} p \\ q \end{pmatrix}$, ha $p\bar{u} + q\bar{v} = \begin{pmatrix} x \\ y \end{pmatrix}$?

A) $\begin{pmatrix} -\frac{3x}{2} \\ y - \frac{7x}{2} \end{pmatrix}$, B) $\begin{pmatrix} -\frac{5x}{2} \\ y - \frac{9x}{2} \end{pmatrix}$, C) $\begin{pmatrix} \frac{x}{2} \\ y - \frac{3x}{2} \end{pmatrix}$, D) $\begin{pmatrix} -\frac{x}{2} \\ y - \frac{5x}{2} \end{pmatrix}$, E) $\begin{pmatrix} \frac{x}{2} \\ y - \frac{3x}{2} \end{pmatrix}$

C