

**Differential equations. Quiz 2.**

Name:

Neptun:

1. Let  $e_1 = \left(\frac{\sqrt{3}i}{2}, \frac{1}{2}\right)^T$ ,  $e_2 = \left(\frac{1}{2}, \frac{\sqrt{3}i}{2}\right)^T$  be an orthonormal basis in  $\mathbb{C}^2$  and let  $u = (3 + i, 4 - 2i)^T$ ,  $u = \alpha_1 e_1 + \alpha_2 e_2$ . Compute  $\alpha_2$  !
2. The characteristic function  $\chi_D$  is defined as  $\chi_D(x) = 0$  if  $x \notin D$ , otherwise  $\chi_D(x) = 1$ . Let  $f(x) = \chi_{[-2,2]}(x)$ ,  $\hat{f}(x) = \sum_{n \in \mathbb{Z}} \hat{f}_n \frac{e^{inx}}{\sqrt{2\pi}}$ . Compute  $\hat{f}_9$  !
3.  $\partial_t \phi(t, x) = \partial_{xx} \phi(t, x)$ ,  $\phi(0, x) = \cos(3\pi x) + 4 \cos(5\pi x)$ . Compute  $\phi(t, x)$  !